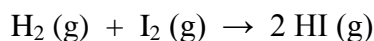


CHEMICAL KINETICS**Chemical Kinetics:**

- I. The study of the Rates of Chemical Reactions:
 - how fast do chemical reactions proceed to form products
- II. The study of Reaction Mechanisms:
 - the steps involved in the change from reactants to products.

I. Rates of Reactions

- Factors affecting Reaction Rates:
 1. Concentration of Reactants: Rate \propto Concentration of Reactants
 2. Presence of a Catalyst: A catalyst is a substance that increases the Reaction Rate without being consumed
 3. Temperature: Rate \propto Temperature
 4. Surface Area of Reactants: Rate \propto Surface Area of Reactants

Definition of Reaction Rate

Reaction Rate:

- increase in the molar concentration of a product per unit time

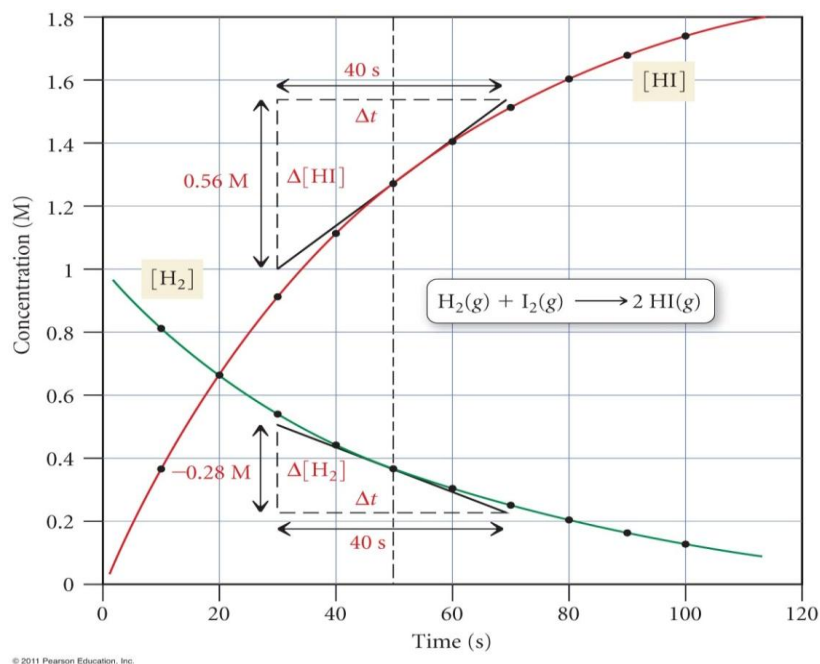
OR

- decrease in the molar concentration of reactant per unit time

$$\text{Rate of disappearance of H}_2 = \frac{\Delta[\text{H}_2]}{\Delta t} = \frac{\text{decrease in the molar conc. of H}_2}{\text{time interval}}$$

- The expression above is referred to as: Average Rate over the time interval Δt

REACTION RATES



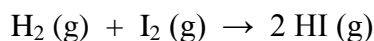
- Reactant concentration decreases with time, while product concentration increases with time.

Time (s)	[H ₂] (M)	Δ[H ₂]	Δt	Rate = -Δ[H ₂]/Δt (M/s)
0.000	1.000	}	}	}
10.000	0.819			
20.000	0.670			
30.000	0.549			
40.000	0.449			
50.000	0.368			
60.000	0.301			
70.000	0.247			
80.000	0.202			
90.000	0.165			
100.000	0.135			

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REACTION RATES

- The Reaction Rate decreases as the reaction proceeds.
Reason: the concentration of reactants decreases
- Any substance in the reaction can be used to express the Rxn. Rate



$$\text{Rate of disappearance of H}_2 = \frac{\Delta[\text{H}_2]}{\Delta t} = \frac{\text{decrease in the molar conc. of H}_2}{\text{time interval}}$$

$$\text{Rate of disappearance of I}_2 = \frac{\Delta[\text{I}_2]}{\Delta t} = \frac{\text{decrease in the molar conc. of I}_2}{\text{time interval}}$$

$$\text{Rate of formation of HI} = \frac{\Delta[\text{HI}]}{\Delta t} = \frac{\text{increase in the molar conc. of HI}}{\text{time interval}}$$

- Reaction Rate is always positive

$$\text{(a) Rate of formation of a product} = \frac{\Delta[\text{increase in concentration of product}]}{\Delta t}$$

$$\text{(b) Rate of decomposition of a reactant} = - \frac{\Delta[\text{decrease in concentration of reactant}]}{\Delta t}$$

Since: $\Delta[\text{decrease in concentration of reactant}]$ has a negative value the Reaction Rate will be positive

4. Reaction Rate in terms of stoichiometry



$$\text{Rate of increase of HI} = 2 \times \text{Rate of decrease of H}_2$$

OR

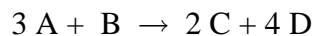
$$\frac{\text{Rate of increase of HI}}{2} = \text{Rate of decrease of H}_2$$

Reason: 2 moles of HI are formed from reaction of 1 mole of H_2

REACTION RATES

Examples:

1. For the hypothetical reaction shown below, write a rate expression based on each reactant and product:



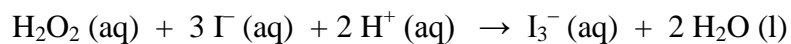
Rate based on A =

Rate based on B =

Rate based on C =

Rate based on D =

2. Consider the following reaction:



In the first 10.0 seconds of the reaction, the concentration of I^- dropped from 1.000 M to 0.868 M.

a) Calculate the average rate of this reaction in this time interval.

b) Predict the rate of change in concentration of H^+ during this time interval.

RATE DETERMINATION

- Rate determination is done by monitoring the change in concentration of reactant or product over time.

Method:

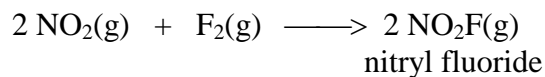
- Withdraw samples from the reaction vessel at various times and analyze some of their physical or chemical properties that give information on the concentrations present.

Properties appropriate and easy to monitor

1. Color
(if product or reactant absorbs light)
3. Oxidation State
(using an electrochemical cell)
5. Volume, at constant p and T
(useful, if:
 - gaseous reactants and/or products are present, and
 - number of moles of reactants \neq number of moles of products))
6. Pressure, at constant V and T
(useful, if:
 - gaseous reactants and/or products are present, and
 - number of moles of reactants \neq number of moles of products))
7. Density
(useful if : $d(\text{reactants}) \neq d(\text{products})$)

Properties not appropriate to monitor

2. Flammability
(difficult to measure quantitatively)
4. Mass
(mass is conserved in a chemical reaction)

RATE LAW
Dependence of Reaction Rate on Concentration


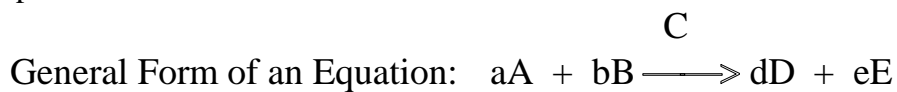
Experimental observation:

$$\text{Rate of Reaction} = k [\text{NO}_2] [\text{F}_2]$$

Meaning: - Doubling $[\text{NO}_2]$ \longrightarrow Doubles the Reaction Rate
 - Doubling $[\text{F}_2]$ \longrightarrow Doubles the Reaction Rate

RATE LAW :

- Equation that relates the Rate of Reaction to the Concentration of Reactants and Catalyst raised to various powers.



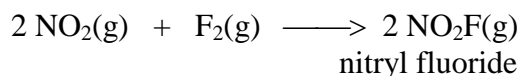
$$\text{General form for Rate Law: } \text{Rate} = k [\text{A}]^m [\text{B}]^n [\text{C}]^p$$

- | | |
|--------------------|--|
| m, n, and p | <ul style="list-style-type: none"> ➤ are frequently, but not always integers ➤ must be determined experimentally ➤ are <u>not</u> the coefficients in the balanced chemical equation |
| k | <ul style="list-style-type: none"> ➤ Rate Constant ➤ its units depend upon the form of Rate Law ➤ depends on temperature |

REACTION ORDER

I. Reaction Order with respect to a given reactant species:

- Reaction Order is the exponent of the concentration of that species in the Rate Law, as determined experimentally



Experimental observation:

- Doubling $[\text{NO}_2]$ \longrightarrow Doubles the Reaction Rate
- Doubling $[\text{F}_2]$ \longrightarrow Doubles the Reaction Rate

$$\text{Rate of Reaction} = k [\text{NO}_2]^m [\text{F}_2]^n$$

Reaction is:

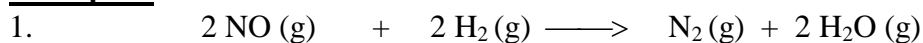
- First order with respect to NO_2 ($m=1$)
- First order with respect to F_2 ($n=1$)

II. Overall Reaction Order

- The overall reaction order is the sum of the orders of the reactant species

$$\text{Overall Reaction Order} = m + n = 1 + 1 = 2$$

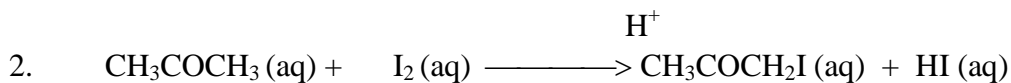
Reaction is of the Second Order Overall.

Examples:

Experimentally determined Rate Law = $k[\text{NO}]^2[\text{H}_2]$

Reaction is:

- 2nd order in NO
- 1st order in H₂
- **3rd order overall**



Experimentally determined Rate Law = $k[\text{CH}_3\text{COCH}_3][\text{H}^+]$

Reaction is:

- 1st order in CH₃COCH₃
- 0 order in I₂ (does not depend on the concentration of I₂ as long as some I₂ is present)
- 1st order in the catalyst (H⁺)
- **2nd order overall**

NOTE: Reaction Orders:

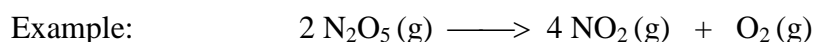
- are frequently whole numbers (1 or 2)
- may be fractional
- may be 0
- may be negative

- Effect of concentration change on reaction rates and orders can be summarized as:

Order	Concentration	Rate
Zero	x 2	No Effect
First	x 2	x 2
Second	x 2	x 4
Negative	x 2	x 1/2
Half	x 2	√2

EXPERIMENTAL DETERMINATION OF RATE LAW

- In determining the rate law for a reaction, first the order of reaction with respect to each reactant and catalyst must be found.
- Commonly a series of experiments are done in which the initial concentrations of reactants are varied (usually doubled).
- The results of these experiments will yield the respective orders of reaction.



	Initial N_2O_5 Conc. (M)	Initial Rate of Disappearance of N_2O_5 (M/s)
Experiment 1	1.0×10^{-2}	4.8×10^{-6}
Experiment 2	2.0×10^{-2}	9.6×10^{-6}

Rate = $k [\text{N}_2\text{O}_5]^m$ $m = ?$ (must be determined from experimental data)

$$\frac{\text{Rate Exp. 2}}{\text{Rate Exp. 1}} = \frac{k (2)^m}{k (1)^m} = \frac{9.6 \times 10^{-6}}{4.8 \times 10^{-6}} = 2$$

Experimental: ➤ Doubling $[\text{N}_2\text{O}_5]$ doubled the rate of reaction

It follows: ➤ $m = 1$ ($2^1 = 2$)

The Reaction is: ➤ First order in N_2O_5
➤ First order overall

$$\text{Rate} = k [\text{N}_2\text{O}_5]^1$$

$$\text{Rate} = k [\text{N}_2\text{O}_5]$$

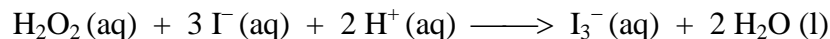
Effect of Doubling the Initial Concentration of Reactant on Reaction Rate

Change in Reaction Rate	Rate is multiplied by	Reaction Order
Rate is halved	$\frac{1}{2} = 2^{-1}$	-1
Rate is the same	$1 = 2^0$	0
Rate is doubled	$2 = 2^1$	1
Rate is quadrupled	$4 = 2^2$	2

Examples:

1. Use the rate data below to

- A) determine the reaction orders with respect to $[\text{H}_2\text{O}_2]$, $[\text{I}^-]$ and $[\text{H}^+]$ and
 B) find the rate constant k for the reaction shown below:



	Initial Concentrations (M)			Initial Rate (M/s)
	$[\text{H}_2\text{O}_2]$	$[\text{I}^-]$	$[\text{H}^+]$	
Experiment 1	0.010	0.010	0.00050	1.15×10^{-6}
Experiment 2	0.020	0.010	0.00050	2.3×10^{-6}
Experiment 3	0.010	0.020	0.00050	2.30×10^{-6}
Experiment 4	0.010	0.010	0.00100	1.15×10^{-6}

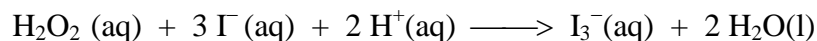
Solution

A) Compare two rate experiments in which all concentrations of reactants but one are held constant:

$[\text{H}_2\text{O}_2]$: Compare **Experiment 1** and **Experiment 2**
When $[\text{H}_2\text{O}_2]$ is doubled, the Rate is doubled
 It follows: $2^m = 2$ $m = 1$ **1st order in $[\text{H}_2\text{O}_2]$**

$[\text{I}^-]$: Compare **Experiment 1** and **Experiment 3**
When $[\text{I}^-]$ is doubled, the Rate is doubled
 It follows: $2^n = 2$ $n = 1$ **1st order in $[\text{I}^-]$**

$[\text{H}^+]$: Compare Experiment 1 and Experiment 4
When $[\text{H}^+]$ is doubled, the Rate does not change
 It follows: $2^p = 1$ $p = 0$ **0 order in $[\text{H}^+]$**



Summary: 1st order in $[\text{H}_2\text{O}_2]$
 1st order in $[\text{I}^-]$
 0 order in $[\text{H}^+]$

$$\text{RATE} = k [\text{H}_2\text{O}_2]^1 [\text{I}^-]^1 [\text{H}^+]^0$$

commonly written :

$$\text{RATE} = k [\text{H}_2\text{O}_2] [\text{I}^-]$$

NOTE: Reaction Orders are **not** related to the coefficients of the overall equation

B) Find the Rate Constant, k

From Experiment 1: (any other experiment could be used)

$$[\text{H}_2\text{O}_2] = 0.010 \text{ M}$$

$$[\text{I}^-] = 0.010 \text{ M}$$

$$\text{Rate} = 1.15 \times 10^{-6} \text{ M/s}$$

$$k = ?$$

$$\text{RATE} = k [\text{H}_2\text{O}_2] [\text{I}^-] \quad k = \frac{\text{Rate}}{[\text{H}_2\text{O}_2][\text{I}^-]} = \frac{1.15 \times 10^{-6} \text{ M/s}}{(0.010 \text{ M})(0.010 \text{ M})} = 1.2 \times 10^{-2} \text{ M}^{-1}\text{s}^{-1}$$

2. Use the rate data below to

A) determine the rate law for the reaction $\text{A} + \text{B} \rightarrow \text{C}$, and

B) calculate the rate constant k, and

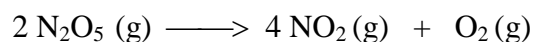
C) calculate the rate of reaction for experiment 4

Experiment Number	[A] (M)	[B] (M)	Initial Rate (M/s)
1	0.100	0.100	4.0×10^{-5}
2	0.100	0.200	4.0×10^{-5}
3	0.200	0.100	16.0×10^{-5}
4	0.050	0.100	????

INTEGRATED RATE LAW (1ST ORDER REACTION)

Concentration – Time Equations for First Order Reactions

- are derived from experimental data
- predict concentrations at all times



$$\text{Rate} = -\frac{\Delta[\text{N}_2\text{O}_5]}{\Delta t} = k [\text{N}_2\text{O}_5]$$

Using calculus:

$$\ln \frac{[\text{N}_2\text{O}_5]_t}{[\text{N}_2\text{O}_5]_0} = -kt$$

OR

$$\log \frac{[\text{N}_2\text{O}_5]_t}{[\text{N}_2\text{O}_5]_0} = \frac{-kt}{2.303}$$

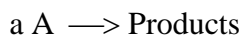
more commonly used!

$[\text{N}_2\text{O}_5]_t$: concentration at time t
 $[\text{N}_2\text{O}_5]_0$: concentration at time 0

These equations can be used to calculate:

- concentration of $[\text{N}_2\text{O}_5]$ at any time,
- the time it takes for $[\text{N}_2\text{O}_5]$ to decrease to a particular value

In General:



Assuming First Order Rate Law:

$$\text{Rate} = k[\text{A}]$$

Differential Rate Law:

$$-\frac{\Delta[\text{A}]}{\Delta t} = k[\text{A}]$$

Integrated Rate Law:

$$\ln \frac{[\text{A}]_t}{[\text{A}]_0} = -kt$$

OR

$$\log \frac{[\text{A}]_t}{[\text{A}]_0} = \frac{-kt}{2.303}$$

Example 1:

Sulfuryl chloride, SO_2Cl_2 , decomposes when heated:



- In an experiment, the initial concentration of SO_2Cl_2 was 0.0248 M
- The Rate Constant is $2.2 \times 10^{-5} \text{ s}^{-1}$. The Reaction is first order.
- What is the concentration of SO_2Cl_2 after 2.5 hours?

$$[\text{A}]_0 = 0.0248 \text{ M} \qquad k = 2.2 \times 10^{-5} \text{ s}^{-1} \qquad t = 2.5 \text{ h (9000 s)}$$

$$\log \frac{[\text{A}]_t}{[\text{A}]_0} = \frac{-kt}{2.303} \qquad \log \frac{[\text{SO}_2\text{Cl}_2]_t}{[\text{SO}_2\text{Cl}_2]_0} = \frac{-kt}{2.303}$$

$$\log \frac{[\text{SO}_2\text{Cl}_2]_t}{[\text{SO}_2\text{Cl}_2]_0} = \frac{-(2.2 \times 10^{-5} \text{ s}^{-1})(9000 \text{ s})}{2.303} = -0.086$$

Take antilogarithms of both sides;

$$\frac{[\text{SO}_2\text{Cl}_2]_t}{[\text{SO}_2\text{Cl}_2]_0} = 0.82 \qquad [\text{SO}_2\text{Cl}_2]_t = (0.82) \times [\text{SO}_2\text{Cl}_2]_0$$

$$[\text{SO}_2\text{Cl}_2]_t = (0.82)(0.0248 \text{ M}) = \mathbf{2.0 \times 10^{-2} \text{ M}}$$

Significant Figures, Logs and Antilogs

Find log of (3.6×10^{-12})

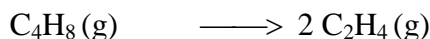
$$\log(3.6 \times 10^{-12}) = -11.44$$

Given: -11.44, find antilog:

$$\text{Antilog} = 10^{-11.44} = 3.6 \times 10^{-12}$$

Example 2:

Cyclobutane, C₄H₈ decomposes, when heated to give ethylene:



- The reaction is first order.
- In an experiment, the initial concentration of C₄H₈ was 0.00150 M.
- After heating at 450°C for 455 seconds, this was reduced to 0.00119 M.
- What was the concentration of C₄H₈ after a total of 827 seconds?

$$[\text{C}_4\text{H}_8]_0 = 0.00150 \text{ M} \quad [\text{C}_4\text{H}_8]_{455} = 0.00119 \text{ M} \quad [\text{C}_4\text{H}_8]_{827} = ?$$

a) Calculate rate constant (k) for the reaction:

$$\log \frac{[\text{C}_4\text{H}_8]_{455}}{[\text{C}_4\text{H}_8]_0} = \log \frac{0.00119 \text{ M}}{0.00150 \text{ M}} = -\frac{k(455 \text{ s})}{2.303} = -197.57 \text{ k}$$

$$\log 0.7933 = -197.57 \text{ k}$$

$$-0.10054 = -197.57 \text{ k}$$

$$\text{k} = 5.089 \times 10^{-4} \text{ s}^{-1}$$

b) Calculate concentration of C₄H₈ at 827 s:

$$\log \frac{[\text{C}_4\text{H}_8]_{827}}{[\text{C}_4\text{H}_8]_0} = -\frac{k(t)}{2.303} = -\frac{(5.089 \times 10^{-4} \text{ s}^{-1})(827 \text{ s})}{2.303} = -0.1827$$

Taking the antilog of both sides:

$$\frac{[\text{C}_4\text{H}_8]_{827}}{[\text{C}_4\text{H}_8]_0} = 0.6566$$

Substituting [C₄H₈]₀

$$\frac{[\text{C}_4\text{H}_8]_{827}}{0.00150 \text{ M}} = 0.6566$$

$$[\text{C}_4\text{H}_8]_{827} = 9.85 \times 10^{-4} \text{ M}$$

HALF-LIFE ($t_{1/2}$) OF A FIRST ORDER REACTION

- Half-life is the time it takes for the reactant concentration to decrease to one-half of its initial value.

$$\log \frac{[A]_t}{[A]_0} = \frac{-k t}{2.303}$$

In one half-life ($t_{1/2}$): $[A]_t = \frac{1}{2} [A]_0 \implies \log \frac{\frac{1}{2} [A]_0}{[A]_0} = \frac{-k (t_{1/2})}{2.303}$

$$-0.301 = \frac{-k (t_{1/2})}{2.303} \implies t_{1/2} = \frac{0.301 \times 2.303}{k}$$

$$t_{1/2} = \frac{0.693}{k}$$

NOTES:

- Half-Life does not depend on the initial concentration, $[A]_0$
- The half-life is the same at any time during the reaction

Example:

Dinitrogen pentoxide, decomposes when heated in carbon tetrachloride solvent:



The rate law is first order in N_2O_5 with a rate constant of $6.2 \times 10^{-4} \text{ min}^{-1}$.

- (a) What is the half-life for this reaction?

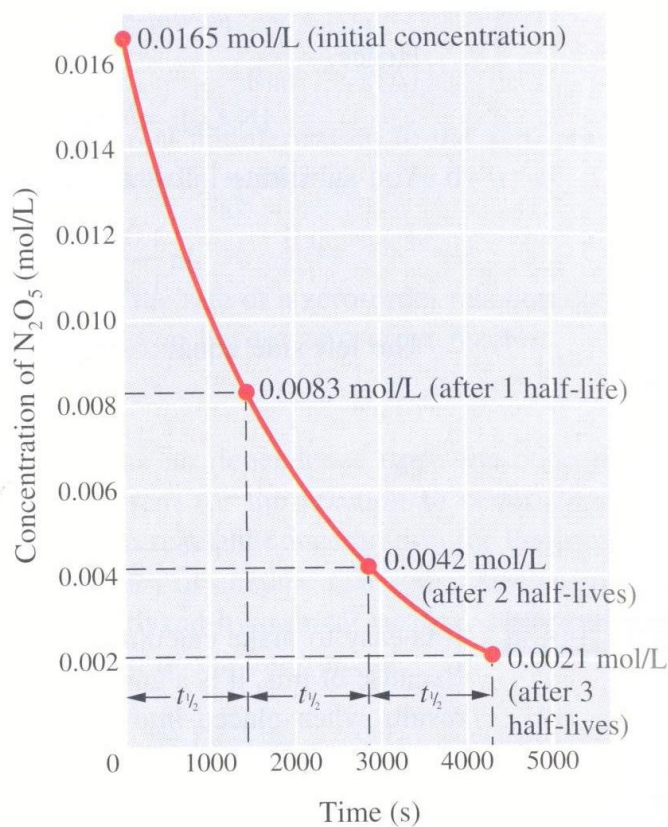
$$t_{1/2} = \frac{0.693}{k} = \frac{0.693}{6.2 \times 10^{-4} \text{ min}^{-1}} = 1118 \text{ min} = 1.1 \times 10^3 \text{ min}$$

- (b) How long would it take for the concentration of N_2O_5 to decrease to 25 % of its initial value?

$$t_{25\% \text{ left}} = t_{1/4 \text{ left}} = 2 \times t_{1/2} = 2 (1.1 \times 10^3 \text{ min}) = 2.2 \times 10^3 \text{ min}$$

- (c) How long would it take for the concentration of N_2O_5 to decrease to 12.5 % of its initial value?

$$t_{12.5\% \text{ left}} = t_{1/8 \text{ left}} = 3 \times t_{1/2} = 3 (1.1 \times 10^3 \text{ min}) = 3.3 \times 10^3 \text{ min}$$



- In each half-life the concentration of the reactant is halved.
- First half-life: concentration changes from 0.016 M to 0.008 M (1440 s)
- Second half-life: concentration changes from 0.008 M to 0.004 M (2880 s)
- Third half-life: concentration changes from 0.004 M to 0.002 M (4320 s)
- **Half-life of first order reactions is independent of concentration**

Concentration (M)	Decrease in Concentration	Time Elapsed (s)	Number of Half-lives Elapsed
0.0120	0	0	0
0.0060	50%	1300	1
0.0030	25%	2600	2
0.0015	12.5%	3900	3
0.00075	6.25%	5200	4

In General:

Concentration	Time	Number of Half-lives
A_0	0	0
$\frac{1}{2} A_0 = 50\% A_0$	$t_{1/2}$	1
$\frac{1}{4} A_0 = 25\%$	$t_{1/4}$	2
$\frac{1}{8} A_0 = 12.5\%$	$t_{1/8}$	3
$\frac{1}{16} A_0 = 6.25\%$	$t_{1/16}$	4

GRAPHING FIRST ORDER REACTIONS

- The order of a reaction can be determined by graphing the experimental data.
- The experimental data are plotted by
 1. First assuming a first-order reaction,
 2. Second, assuming a second-order reaction,
 3. Third, assuming a third-order reaction, and so on.
- The graph which best fits the experimental data gives the order of a reaction.

- First order Rate Law:

$$\log \frac{[A]_t}{[A]_0} = \frac{-k t}{2.303}$$

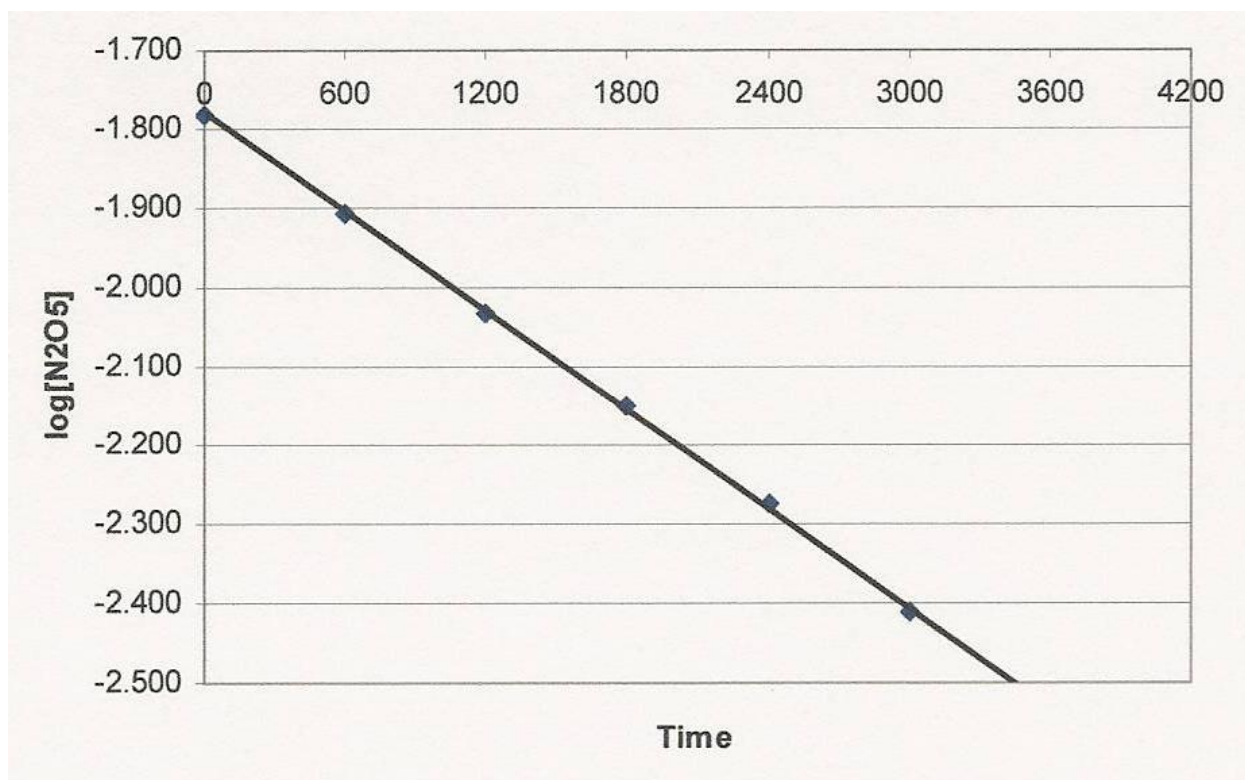
- This equation may be rewritten:

$$\log [A]_t = \left(\frac{-k t}{2.303} \right) + \log [A]_0 \quad (\text{This is the equation of a straight line})$$

$$\log [A]_t = \left(\frac{-k}{2.303} \right) t + \log [A]_0 \quad y = mx + b$$

- A plot of **log [A]** (y) versus **time** (x) should give a straight line for a first order reaction.

Time	[N ₂ O ₅]	log [N ₂ O ₅]
0	0.0165	-1.783
600	0.0124	-1.907
1200	0.0093	-2.032
1800	0.0071	-2.149
2400	0.0053	-2.276
3000	0.0039	-2.409
3600	0.0029	-2.538



- NOTE: The points lie on a straight line
- MEANING: The Rate Law is First Order

$$m = \text{slope of the straight line} = \frac{\Delta y}{\Delta x} = \frac{(-2.538) - (-1.783)}{(3600 - 0) \text{ s}} = \frac{-0.755}{3600 \text{ s}} = -2.10 \times 10^{-4} \text{ s}^{-1}$$

This can be used to calculate k , the Rate constant

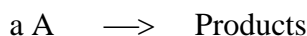
Recall: $\log [A]_t = \left(\frac{-k t}{2.303} \right) + \log [A]_0$ $y = mx + b$

It follows:

$$m = \frac{-k}{2.303} \qquad k = -2.303 (-2.10 \times 10^{-4} \text{ s}^{-1}) = 4.84 \times 10^{-4} \text{ s}^{-1}$$

INTEGRATED RATE LAW (2ND ORDER REACTION)

Concentration – Time Equations for First Order Reactions



$$\text{Rate} = -\frac{\Delta [A]}{\Delta t} = k [A]^2$$

Differential Rate Law

By using calculus:

$$\frac{1}{[A]_t} = kt + \frac{1}{[A]_0}$$

Integrated Rate Law

Example:

1. For the reaction



At 330 K:

$$k = 0.775 \text{ M}^{-1}\text{s}^{-1}$$

$$[A]_0 = 0.0030 \text{ M}$$

$$[A]_{645} = ?$$

$$\frac{1}{[A]_t} = (0.775 \text{ M}^{-1}\text{s}^{-1})(645 \text{ s}) + \frac{1}{0.0030 \text{ M}}$$

$$\frac{1}{[A]_t} = (499.9 \text{ M}^{-1}) + (333.3 \text{ M}^{-1}) = 8.3 \times 10^2 \text{ M}^{-1}$$

$$[A]_t = 0.0012 \text{ M}$$

HALF-LIFE ($t_{1/2}$) OF A SECOND ORDER REACTION

- Half-life is the time it takes for the reactant concentration to decrease to one-half of its initial value.

For a second order reaction: Rate = $k [A]^2$ and $\frac{1}{[A]_t} = kt + \frac{1}{[A]_0}$

In one half-life ($t_{1/2}$): $[A]_t = \frac{1}{2} [A]_0$ \Rightarrow $\frac{1}{0.5[A]_0} = kt + \frac{1}{[A]_0}$

$$kt_{1/2} = \frac{1}{0.5[A]_0} - \frac{1}{[A]_0} = \frac{1}{[A]_0} \quad \Rightarrow \quad \boxed{t_{1/2} = \frac{1}{k [A]_0}}$$

NOTES:

- Half-Life depends on the initial concentration, $[A]_0$
- Half-Life increases as reaction progresses

Example:

1. For a particular 2nd order reaction $k = 0.775 \text{ M}^{-1}\text{s}^{-1}$.

a) How long does it take to the concentration to decrease from 0.0030 M to 0.0015?

For concentration to drop to half of its original value, $t = \text{half-life}$

$$t_{1/2} = \frac{1}{k [A]_0} = \frac{1}{(0.775 \text{ M}^{-1}\text{s}^{-1})(0.0030 \text{ M})} = 430 \text{ s}$$

b) How long does it take for the concentration to be halved again?

$$t_{1/2} = \frac{1}{k [A]_0} = \frac{1}{(0.775 \text{ M}^{-1}\text{s}^{-1})(0.0015 \text{ M})} = 860 \text{ s} \quad \leftarrow \text{Twice as long}$$

GRAPHING SECOND ORDER REACTIONS

$$\begin{array}{c}
 \boxed{\frac{1}{[A]_t}} = \boxed{k} \boxed{t} + \boxed{\frac{1}{[A]_0}} \\
 \uparrow \qquad \quad \uparrow \quad \uparrow \qquad \quad \uparrow \\
 \text{y} \qquad \quad = \text{m x} + \text{b} \\
 \uparrow \qquad \quad \uparrow \qquad \quad \uparrow \\
 \text{slope} \qquad \quad \text{intercept}
 \end{array}$$

Meaning:

- A plot of $\frac{1}{[A]_t}$ (y) versus time (s) should give a straight line for a second order reaction

Summary:

To determine the order of a reaction,

1. Collect time vs. concentration data for the reaction.
2. Assuming 1st order, plot log [A] vs. time.
3. If a linear graph is obtained, then it is 1st order.
4. If no linear graph, then plot 1/[A] vs. time.
5. If a linear graph is obtained, then it is 2nd order.

Example:

1. Given the experimental data listed below, determine if the reaction is 1st or 2nd order, and determine the rate constant (k) for the reaction shown below:



Time (s)	[NO ₂] ₀ (M)
0	1.00 x 10 ⁻²
60	0.683 x 10 ⁻²
120	0.518 x 10 ⁻²
180	0.418 x 10 ⁻²
240	0.350 x 10 ⁻²
300	0.301 x 10 ⁻²
360	0.264 x 10 ⁻²

Strategy:

- We must first see if the data fits the Rate Law for 1st Order Reactions. If it does, the reaction is of the 1st order
- If it does not, we must see if the data fits the Rate Law for 2nd Order. If it does, the reaction is of the 2nd order

First Order Rate Law:

$$\log [A]_t = \left(\frac{-k t}{2.303} \right) + \log [A]_0$$

Plot $\log [A]_t$ as a function of t

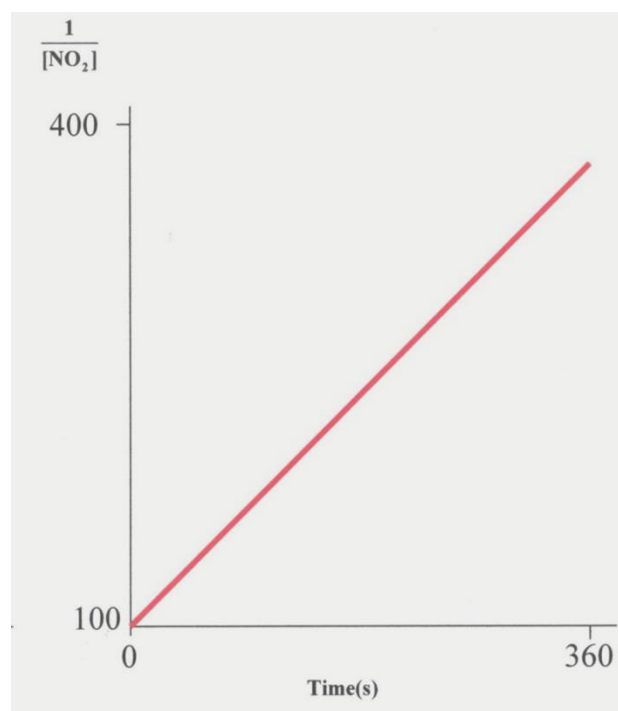
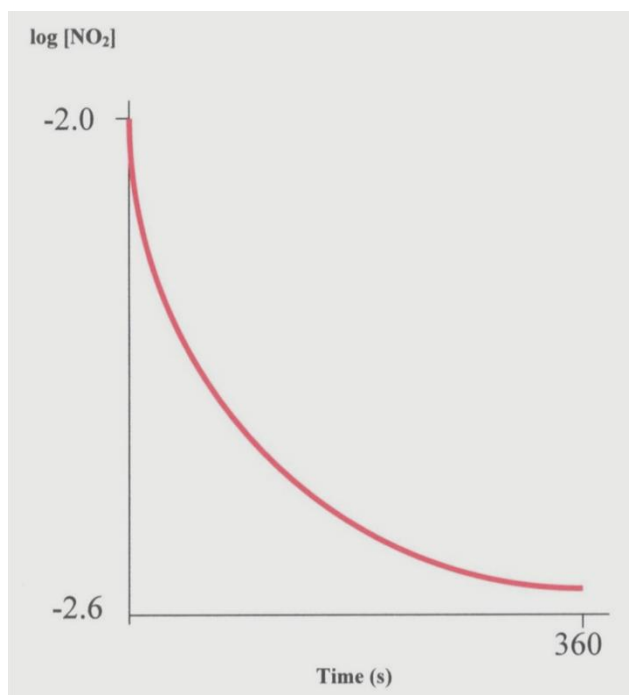
$y = m x + b$

Second order Rate Law

$$\frac{1}{[A]_t} = k t + \frac{1}{[A]_0}$$

Plot $1/[A]_t$ as a function of t

Time (s)	[NO ₂] ₀ (M)	$\log [A]_t$	$1/[A]_t$ (M ⁻¹)
0	1.00 x 10 ⁻²	-2.000	100
60	0.683 x 10 ⁻²	-2.166	146
120	0.518 x 10 ⁻²	-2.286	193
180	0.418 x 10 ⁻²	-2.379	239
240	0.350 x 10 ⁻²	-2.456	286
300	0.301 x 10 ⁻²	-2.521	332
360	0.264 x 10 ⁻²	-2.2578	379



- Not a straight line
- Reaction is not of 1st Order

- A straight line is obtained
- **Reaction is of 2nd Order**

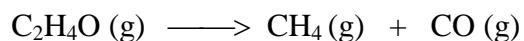
$$k = \text{slope} = \frac{\Delta y}{\Delta t} = \frac{(379 - 100) \text{ M}^{-1}}{(360 - 0)} = 0.775 \text{ M}^{-1} \text{ s}^{-1}$$

SUMMARY OF KINETICS EQUATIONS

Order	Rate Law	Differential Rate Law	Integrated Rate Law	Half-Life	Graphical Plot for a Straight Line
0	k	$-\frac{\Delta[A]_t}{\Delta t} = k$	$[A] = -k t + [A]_0$	$\frac{[A]_0}{2 k}$	[A] vs. t
1	Rate = k [A]	$-\frac{\Delta[A]_t}{\Delta t} = k [A]$	$\log \frac{[A]_t}{[A]_0} = -\frac{kt}{2.303}$ or $\log [A]_t = \left(\frac{-k t}{2.303}\right) + \log [A]_0$	$\frac{0.693}{k}$	log [A] vs. t
2	Rate = k [A] ²	$-\frac{\Delta[A]_t}{\Delta t} = k [A]^2$	$\frac{1}{[A]_t} = k t + \frac{1}{[A]_0}$	$\frac{1}{k[A]_0}$	$\frac{1}{[A]_0}$ vs. t

Examples:

1. Ethylene oxide, C₂H₄O(g), decomposes when heated to give methane and carbon monoxide:



The following kinetic data were observed for the reaction at 688K

	[C ₂ H ₄ O] ₀ (M)	Initial Rate (M/s)
Experiment 1	0.00272	5.57 x 10 ⁻⁷
Experiment 2	0.00544	1.11 x 10 ⁻⁶

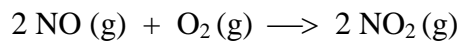
Find the Rate Law and the value of the Rate Constant.

Rate =

k =

Examples:

3. In a kinetic study of the reaction shown below, the following data were obtained for the initial rates of disappearance of NO and O₂ :



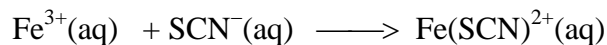
	[NO] ₀ (M)	[O ₂] ₀ (M)	Initial Rate (M/s)
Experiment 1	0.0125	0.0253	0.0281
Experiment 2	0.0250	0.0253	0.112
Experiment 3	0.0125	0.0506	0.0561

Obtain the Rate Law and the Rate Constant.

Rate =

k =

4. In the presence of excess thiocyanate ion (SCN⁻) the following reaction is 1st order with respect to Fe³⁺ with a rate constant of 1.27 s⁻¹.



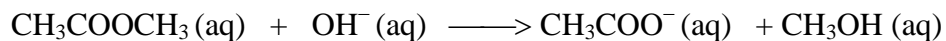
- a) What is the Half-Life in seconds?

t_{1/2} =

- b) How many seconds would be required for the initial concentration of Fe³⁺ to decrease to each of the following values? (25.0 % and 12.5 %)

- c) How many seconds are required for 90.0% of reaction to be completed?

5. Methyl acetate ($\text{CH}_3\text{COOCH}_3$) reacts in basic solution to give acetate ion (CH_3COO^-) and methanol (CH_3OH).



The overall order of reaction was determined by starting with methyl acetate, $\text{CH}_3\text{COOCH}_3$ and hydroxide ion, OH^- , at the same concentrations, so $[\text{CH}_3\text{COOCH}_3] = [\text{OH}^-] = x$.

Then $\text{Rate} = k [\text{CH}_3\text{COOCH}_3]^m [\text{OH}^-]^n = k x^{m+n}$

Determine the overall order and the value of the rate constant by plotting data assuming first- and then second-order kinetics.

Time (min)	$[\text{CH}_3\text{COOCH}_3]$ (M)		
0.00	0.01000		
3.00	0.00740		
4.00	0.00683		
5.00	0.00634		

TEMPERATURE AND RATE

- The Rate of Reaction depends on Temperature.

Recall:

- k (rate constant) is temperature dependent.
- In most cases k increases with temperature



<u>Temperature</u>	<u>k</u>
25 ⁰ C	4.9 x 10 ⁻⁶ M ⁻¹ s ⁻¹
35 ⁰ C	15 x 10 ⁻⁶ M ⁻¹ s ⁻¹

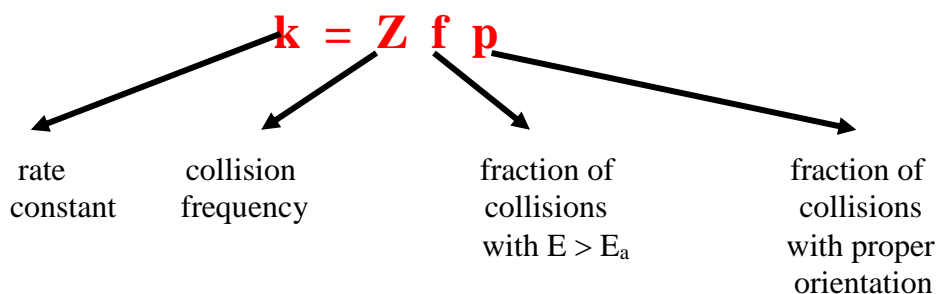
NOTE:

- In this case, “**k**” (the Rate Constant) is more than tripled for a 10⁰ C increase in temperature.
- Consequently, for this reaction, the Reaction Rate is also more than tripled for a 10⁰ C increase in temperature.

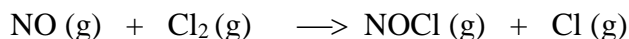
Why?

COLLISION THEORY

- Collision theory states that for a reaction to occur, the reactant molecules must collide:
 - with an **energy** greater than some minimum value, called Activation Energy (E_a)
 - and
 - with the **proper orientation**
 - **“k”** is shown to depend on 3 factors:



For the previous example:



Z = collision frequency – (depends on temperature)

- (As “**t**” increases \longrightarrow molecules move faster \longrightarrow molecules collide more often)
- Root-mean-square (r m s) \approx average molecular speed = u

$$u = \sqrt{\frac{3RT}{M_m}}$$

- This relationship shows that :
 - At 25°C , a 10°C increase in temperature, increases Z by 2 %
 - This does not explain the large increase in rate with temperature

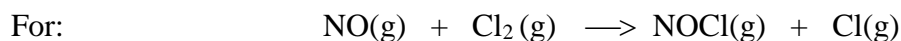
f = fraction of molecules with $E > E_a$

$$f = e^{-\frac{E_a}{RT}}$$

$$e = 2.718$$

$$R = 8.31 \text{ J/molK}$$

$$E_a = 8.5 \times 10^4 \text{ J/mol}$$



At : 25°C (298K) $f = 1.2 \times 10^{-15}$

35°C (308) $f = 3.8 \times 10^{-15}$

NOTE:

1. “f” triples with a 10°C increase in temperature

2. The Effect of E_a is impressive:

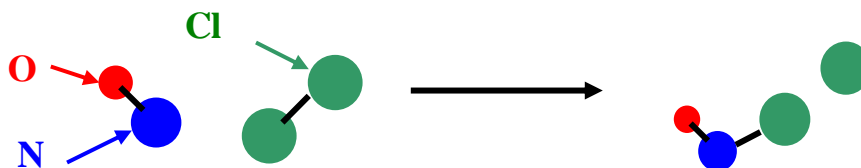
- If E_a is large \longrightarrow “f” is small \longrightarrow “k” is small \longrightarrow reaction is slow
- If E_a is small \longrightarrow “f” is large \longrightarrow “k” is large \longrightarrow reaction is fast

p = fraction of collisions with proper orientation

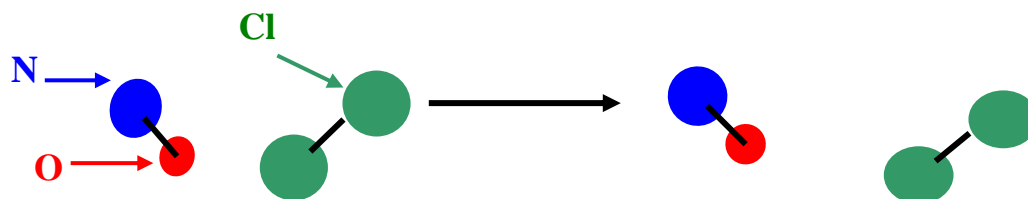
- The only effective orientation is the one in which:

- The NO molecules approaches with N atom toward Cl_2
- The angle of approach is about that expected for the formation of bonds in NOCl (slightly less than 120°)

- See below an effective orientation:

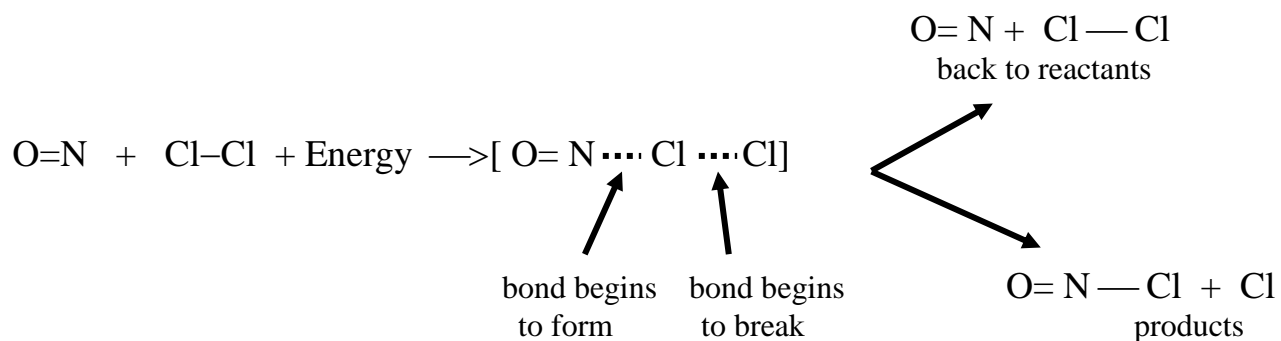


- All other orientations will result in ineffective collisions:



TRANSITION STATE THEORY

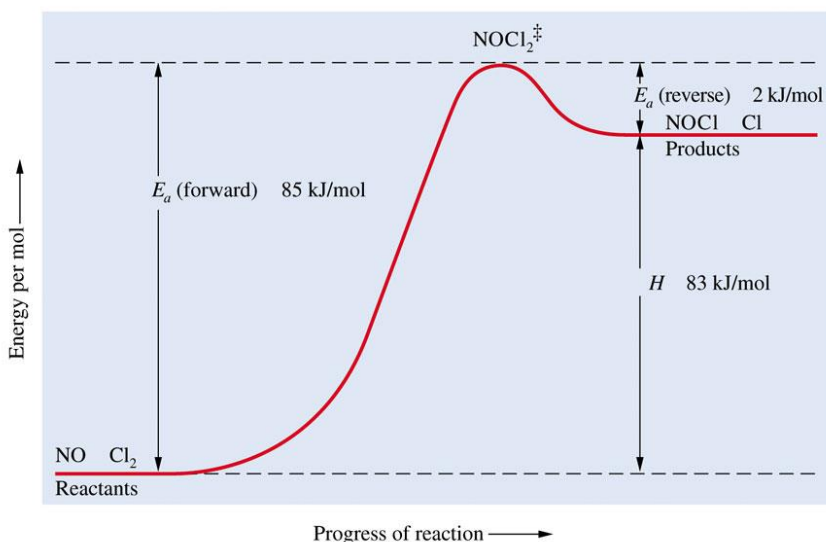
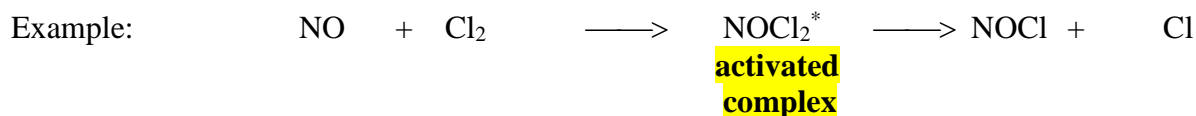
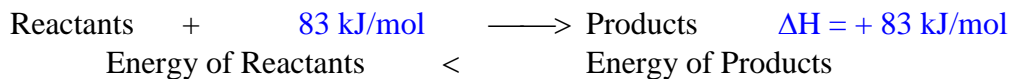
- This theory explains the reaction resulting from the collision of 2 molecules, in terms of an *activated complex*.
- An Activated Complex (*Transition State*) is an unstable grouping of atoms that can break up to form products:



- Which bond breaks depends on where the absorbed energy is concentrated.

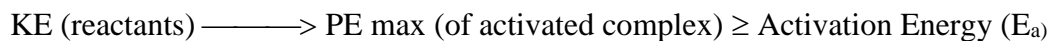
POTENTIAL – ENERGY DIAGRAMS FOR REACTIONS

I. Endothermic Reactions



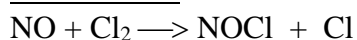
NOTES:

- Sum of (Kinetic Energy + Potential Energy) is constant throughout the reaction. (Law of Conservation of Energy)
- From: Reactants \longrightarrow Activated Complex
(NO + Cl₂) \longrightarrow (NOCl₂^{*})
 - Potential Energy increases (outer electrons of molecules repel, as molecules get closer)
 - Kinetic Energy decreases (molecules slow down)
 - Kinetic Energy changes into Potential Energy
- The reaction will yield product only if : PE(max) \geq Activation Energy (E_a). This will only occur if reactant molecules possess sufficient KE to start with.



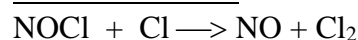
- Comparing the forward and the reverse reactions.

Forward Rxn



E_a = 85 kJ/mol
k is much smaller
Reaction is much slower

Reverse Reaction



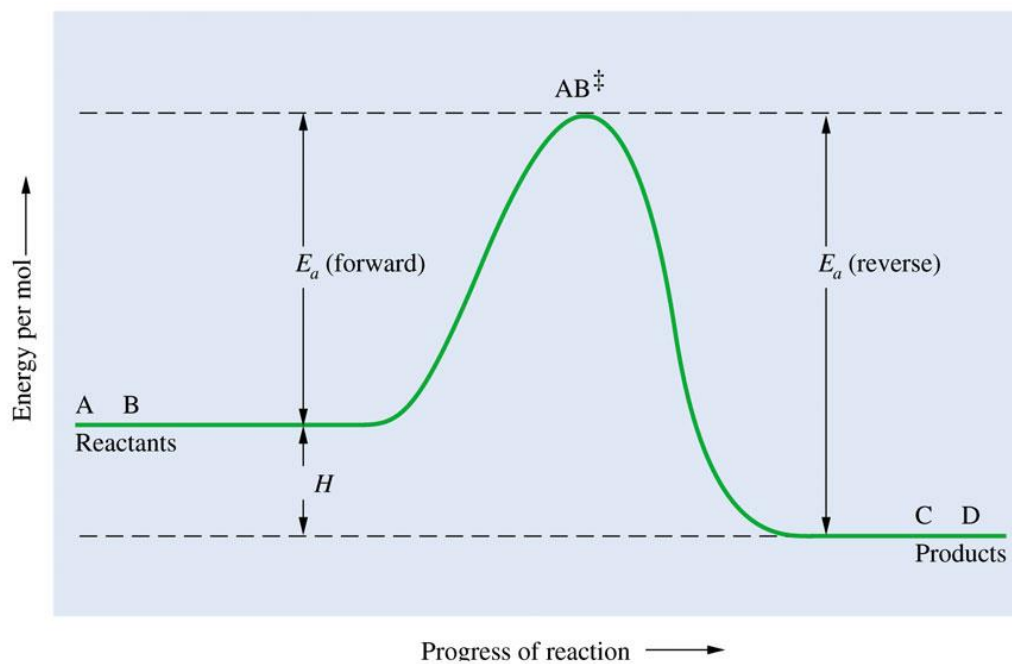
E_a = 2 kJ/mol
k is much larger
Reaction is much faster

II. Exothermic Reactions

Reactants $- \Delta H \longrightarrow$ Products ΔH is negative

Energy of Reactants $>$ Energy of Products

Example: $A + B \longrightarrow C + D + \text{Energy}$



ARRHENIUS EQUATION

$$k = A e^{-\frac{E_a}{RT}}$$

$$e = 2.718$$

E_a = Activation Energy

R = gas constant = 8.31 J/K x mol

T = absolute temperature

A = frequency factor

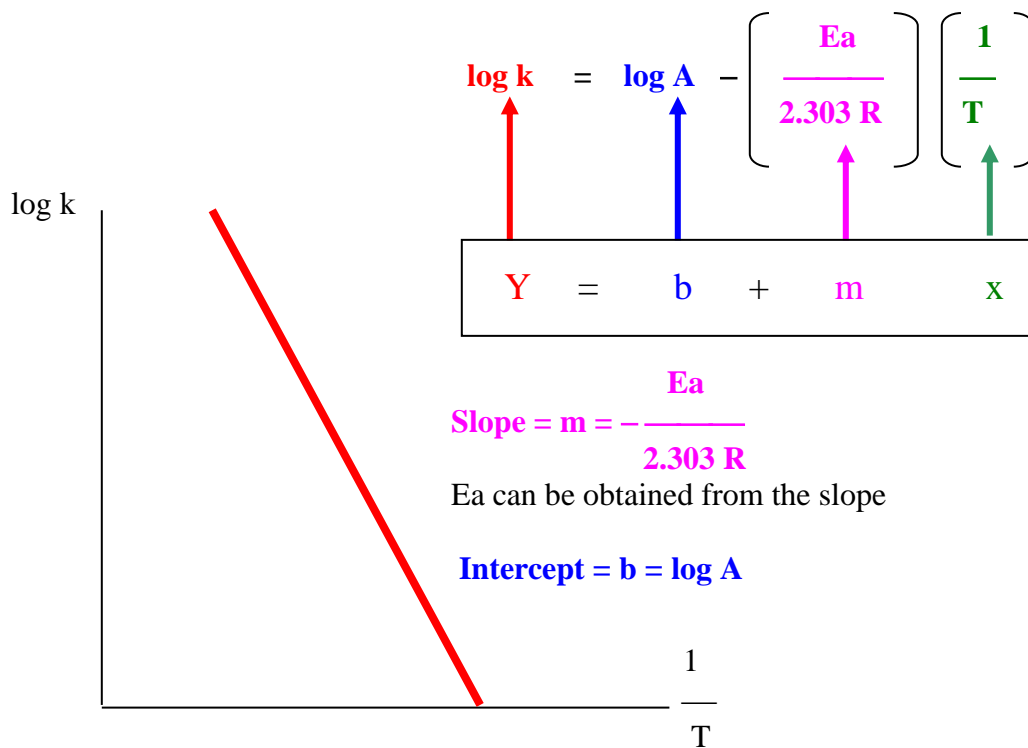
- The equation expresses the dependence of k on temperature.

A = frequency factor

- A is related to the frequency of collisions (Z) with proper orientation (p)
- A depends slightly on temperature (but can be ignored)

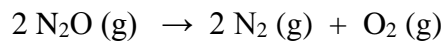
$$\ln k = \ln A - \frac{E_a}{RT}$$

$$\log k = \log A - \frac{E_a}{2.303 RT}$$



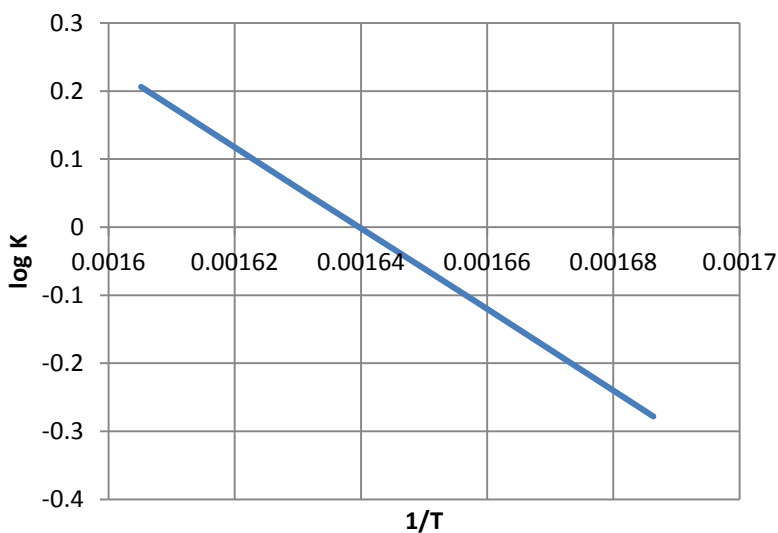
Examples:

1. Sketch a potential energy diagram for the decomposition of nitrous oxide:



The activation energy for the forward reaction is 251 kJ; the ΔH° is +167 kJ. What is the activation energy for the reverse reaction? Label the diagram appropriately.

2. The rate constant for a particular reaction was studied at various temperatures and a plot of $\log k$ vs. $1/T$ was obtained as shown below. Determine the activation energy of this reaction based on the graph below.

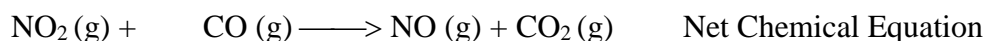


REACTION MECHANISMS

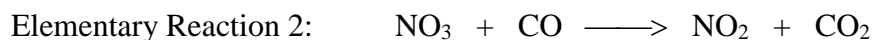
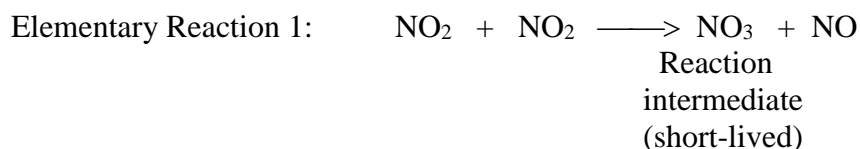
- Reaction Mechanisms show the steps involved in the change from Reactants to Products
- Mechanisms consist of a set of “**Elementary Reactions**” whose overall effect is the Net Chemical Equation.

Elementary Reactions:

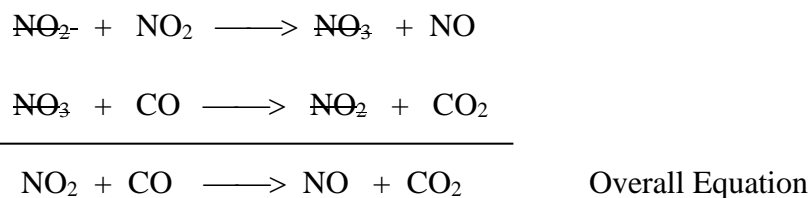
- **Elementary reactions** are single molecular events that result in a reaction and are caused by molecular collisions



Below 500K, this reaction takes place in 2 steps:



- Adding the steps (Elementary Reactions) yields the Overall Equation:


Example 1:

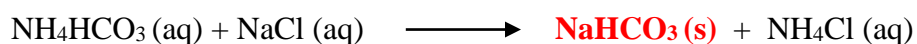
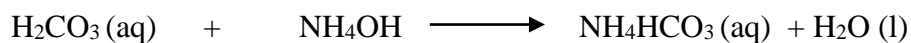
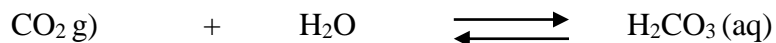
The decomposition of Ozone (O_3) is believed to occur in 2 steps:



Identify any Reaction Intermediate:
What is the Overall equation?

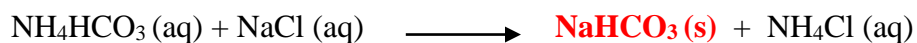
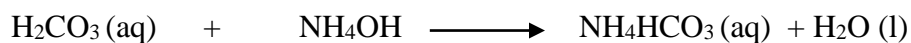
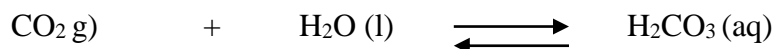
Example 2:

Sodium hydrogen carbonate (**NaHCO₃**), also called sodium bicarbonate can be synthesized through a sequence of 3 elementary steps:



Identify the Reaction Intermediates:

Write the Overall Equation:

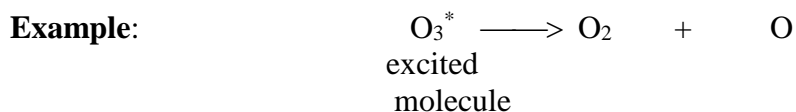


MOLECULARITY

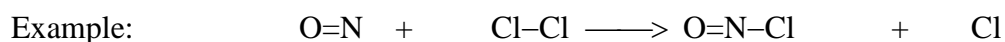
- **Molecularity** is the number of molecules on the reactant side of an Elementary Reaction.

Unimolecular Reactions:

- **Unimolecular** reactions are Elementary Reactions that involve **ONE** reactant molecule.
- These are commonly the decomposition reactions of unstable species.


Bimolecular Reactions:

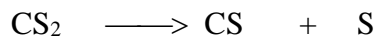
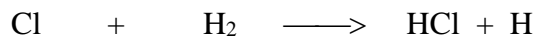
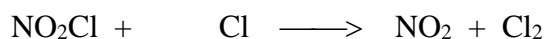
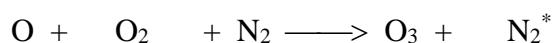
- Bimolecular reactions are Elementary Reactions that involve **TWO** reactant molecules.
- These are very common reactions.


Termolecular Reactions:

- **Termolecular** reactions are Elementary Reactions that involve **THREE** reactant molecules.
- These are less common because the chance of three molecules coming together with the right orientation is unlikely.

Example 1:

What is the molecularity of each of the following elementary reactions?



Rate Equation for an Elementary ReactionI. For an Overall Reaction, the Rate Law cannot be predicted by the Overall Equation

Reasons:

- The majority of reactions consist of several elementary steps.
- The Rate Law is the combined result of the elementary steps
- The rate of all the elementary reactions must be known in order to predict the rate law for the overall equation.

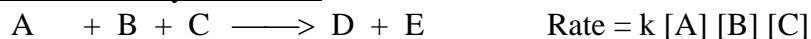
II. For an Elementary Reaction, the Rate Law can be written directly from the Elementary Equations

- The rate of an elementary reaction is proportional to the product of the concentrations of each reactant molecule.

1. Unimolecular Elementary Reactions2. Bimolecular Elementary Reactions

Reason:

- The frequency of collisions is proportional to the number of A molecules (n_A) and the number of B molecules (n_B)

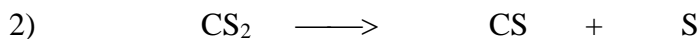
3. Termolecular Elementary Reactions**Examples:**

Write Rate Equations for each of the elementary reactions shown below

:



Rate =



Rate =



Rate =

NOTE:

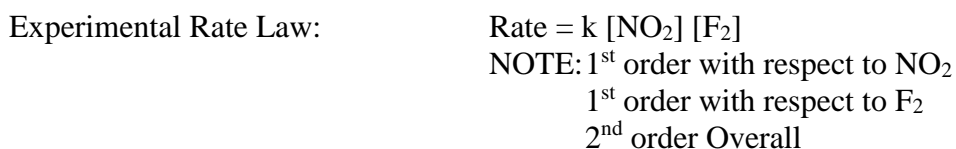
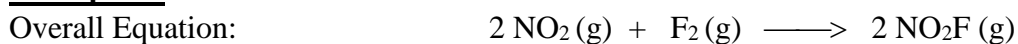
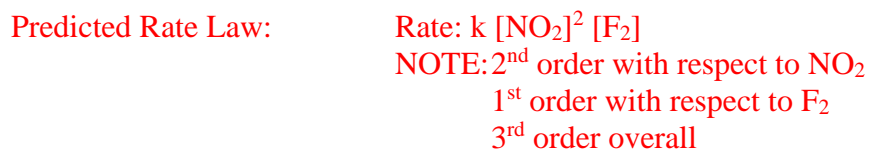
- For Elementary Reactions **ONLY**, the coefficients of the balanced chemical elementary reaction are the exponents to which the concentrations of the reactants are raised.

THE RATE LAW AND THE MECHANISM

- The Suggested Mechanism for a particular reaction:
 - cannot be observed directly,
 - is a rationalized explanation based on experimental data,
 - is accepted provisionally, and may be replaced by another suggested mechanism based on further experimentation.

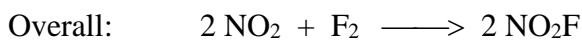
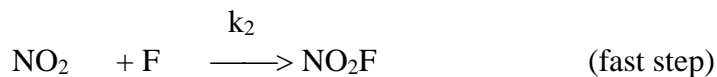
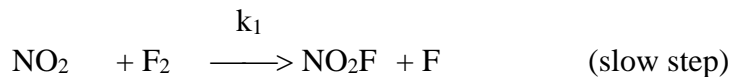
- A Suggested Mechanism

<ul style="list-style-type: none"> ➤ Is considered correct if it agrees with the experimentally determined Rate Law 	<ul style="list-style-type: none"> ➤ Is considered incorrect if it does not agree with the experimentally determined Rate Law
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Example 1:

Predicted Possible Mechanisms:
1. One Single Elementary Reaction


- The predicted Rate Law does not agree with the experimental Rate Law
- This mechanism must be incorrect.

2. Two Single Elementary Reactions



Reaction Intermediate: F

NOTE:

- The Rate Law is determined by the slow step
- **THE SLOWEST STEP —→ THE RATE DETERMINING STEP**
- Predicted Rate Law = RATE (rate-determining-step) = $k_1[\text{NO}_2][\text{F}_2]$

NOTE: 1st order with respect to NO₂
 1st order with respect to F₂
 2nd order overall

- The predicted Rate Law agrees with the experimental Rate Law
- This mechanism must be correct.

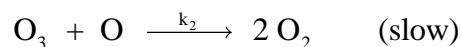
Predicted Rate Law
 RATE = $k_1[\text{NO}_2][\text{F}_2]$

Experimental Rate Law
 RATE = $k[\text{NO}_2][\text{F}_2]$

The two Rate Laws are identical if: $k_1 = k$

Example 2:

The following mechanism has been proposed for decomposition of ozone to oxygen gas:



Determine the Rate Law based on this mechanism.

CATALYSIS

- A **Catalyst** is a substance that speeds up a reaction without being consumed.
- In theory the catalyst may be used over and over again.
- In practice, however, there is some loss of catalyst through other reactions that occur at the same time (side-reactions).

Importance of Catalysts:

- Catalysts allow reactions to occur much faster.
- Catalysts allow reactions to occur at lower temperatures (energy savings).

Characteristics of Catalysts:

- Catalysts are often quite specific. They increase the rate of some reactions but not others.
- Enzymes (catalysts used in biological organisms) are extremely selective.

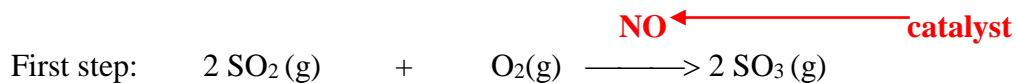
How Catalysts Work:

- A catalyst is an active participant in the reaction.
- A catalyst must participate in one step of a reaction and be regenerated in a later step.
- The catalyzed reaction mechanism makes available a reaction path having an **increased overall rate of reaction** by:
 - increasing the frequency factor A, or
 - decreasing the **Activation Energy, Ea** (most dramatic effect)

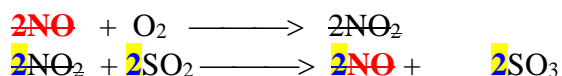
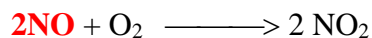
$$k = A e^{-\frac{E_a}{RT}}$$


Examples:

1. The commercial preparation of sulfuric acid, H_2SO_4 from SO_2 (the early process)

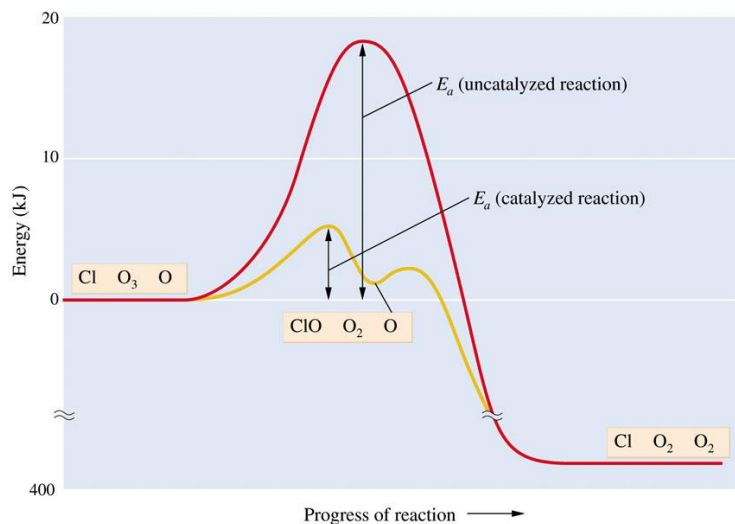
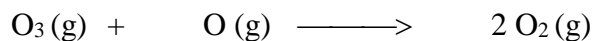
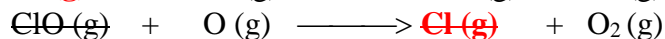
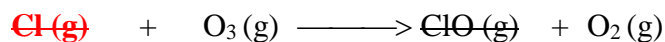


Proposed Mechanism:



2. The Cl-catalyzed decomposition of ozone (O_3) in the stratosphere

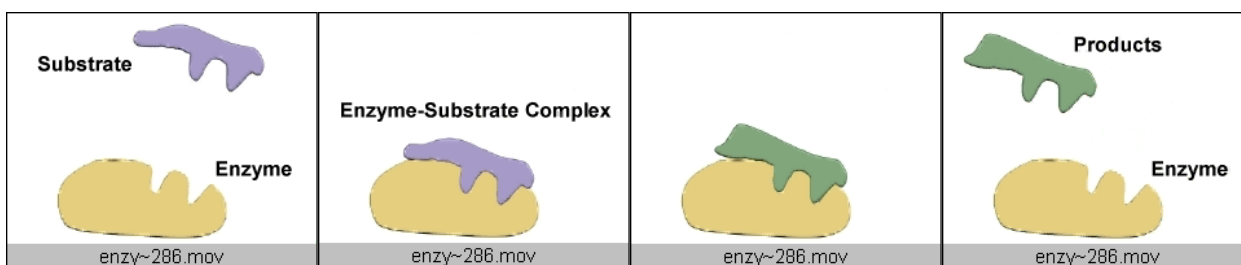
(Cl atoms originate from the decomposition of chloro-fluorocarbons, compounds used as refrigerants and aerosol propellants)

Mechanism of catalyzed reaction:

ENZYME CATALYSIS

- **Enzymes** are the catalysts of biological organisms.
- Enzymes are huge protein molecules (Molecular Weights over a million amu) that are **highly specific**:
 - Each enzyme acts only on a **specific substance** or a **specific type of substance**.
 - Each enzyme catalyzes a **specific substance** to undergo a **specific reaction**.
- Substrate (S) is the substance whose reaction the enzyme catalyzes.

How an enzyme (E) works



The enzyme molecule folds into a roughly spherical shape with an active site	Substrate molecule and enzyme molecule fit into each other like a lock and key	Substrate changes into products, and they diffuse away and the enzyme is regenerated
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